Implicit Modeling

Implicit Surface Representation

• Surface is where level set function is zero $\phi(x, y) = 0$



Signed distance function (SDF) is a common choice of level-set function

Level-set Function Practice

Check it out!

• What function become on the red curves 0?



Constructive Solid Geometry (CSG)

• Modeling shape with *boolean* operation



Try OpenSCAD! https://openscad.org/



Mesh vs Implicit Representation

mesh representation



implicit representation





mesh surgery!

 $f(x, y) = \min(CircleA, CircleB)$

Implicit Modeling in Engineering

- Lattice structure designed by nTopology
- Useful in aerospace, implants design, heat transfer...etc



nTop Live: What is Implicit Modeling in nTopology https://www.youtube.com/watch?v=7HidZ9dHi5M

Ray Casting

Shooting ray from camera



Sphere Tracing Algorithm

• Ray marching using *signed distance function (SDF)*



Hart, John C.. "Sphere tracing: a geometric method for the antialiased ray tracing of implicit surfaces." The Visual Computer 12 (1996): 527-545.

Normal of Implicit Surfaces

• Gradient of implicit function sives normal



Level-set Function on a Regular Grid

• Define value on a vertices of the grid



Implicit Surface to Mesh: Marching Cube



Implicit Surface to Mesh: Marching Cube

15 patterns of signs at 8 vertices















Image Credit: Jmtrivial @ Wikipedia



Image from Wikipedia

Metaball

$$\phi(\vec{p}) = \left(\sum_{i=1}^{N} \psi(|\vec{p} - \vec{q}_i|)\right) - \alpha$$



Image Credit: GlydeG @ Wikipedia

Meatball vs Metaball

https://wikidiff.com/metaball/meatball

